

List k -fold coloring cycles with Hall's condition

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Abstract

The k -fold Hall number of a graph G , $\chi_k(G)$, is the minimum positive integer m such that if L is any list assignment with $|L(v)| = m$ for every $v \in V(G)$ then there is a k -fold list coloring of G whenever G and L satisfy Hall's condition (a natural necessary condition). Here we shall investigate this parameter for cycles. Specifically we determine that for all cycles with equality when n is odd and demonstrate an arrangement showing $\chi_k(C_n) = \lceil \frac{n}{k} \rceil$. As a corollary of these results we obtain combinatorial proofs for the values of the k -fold choice number of cycles.

Keywords: Hall's condition, list coloring, k -fold coloring (list), multicoloring.