

JZsp01

PROGRAM : IEULER2

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PURPOSE : To draw an approximate trajectory in the (phase-) xy -plane for the autonomous system $x' = f(x,y)$, $y' = g(x,y)$. The method used is the *Improved Euler algorithm*:

$$\begin{cases} x_{i+1} = x_i + \frac{f(x_i, y_i) + f(u_i, v_i)}{2} h \\ y_{i+1} = y_i + \frac{g(x_i, y_i) + g(u_i, v_i)}{2} h \end{cases} \quad \text{where} \quad \begin{cases} u_i = x_i + f(x_i, y_i)h \\ v_i = y_i + g(x_i, y_i)h \end{cases}$$

PLATFORM: Texas Instruments TI 82/83 graphing calculator

Input : The user is prompted for the starting values t_0 , x_0 , and y_0 and stepsize h

The functions $f(t,x,y)$ and $g(t,x,y)$ are specified in Y_2 and Y_3 resp.

Output: a graph of the xy -plane showing the approximate trajectory starting at t_0 , x_0 , and y_0 .

Note: to halt the program, press the OFF key.

PROGRAM IEULER2

COMMAND LOCATION

:FnOff

:Prompt X

Prompt: PRG I/O 2

:Prompt Y

:Prompt H

:Lbl P

:X A

:Y B

:T C

:Y₂ U

:Y₃ V

:X+HU X

:Y+HV Y

:A+H(U+Y₂)/2 X

:B+H(V+Y₃)/2 Y

:Line(A,B,X,Y)

Line: DRAW 2

:Goto P